Mathematics MAT 305 : Fundamental Structures of Mathematics Fall 2006

MF 12:30 p.m. - 1:45 p.m., Room 240

Instructor: Dr. Brad Emmons Office: DePerno Hall 121 Telephone: 792-3413 Office Hours: Tuesday 9:30 - 10:20, Wednesday 11:30 - 12:20, Thursday, 1:00 - 2:00 Email: bemmons@utica.edu Homepage: http://www.utica.edu/faculty_staff/bemmons

Course Materials

A Transition to Advanced Mathematics, Sixth Edition, Smith, Eggen, St. Andre (required)

Introduction

This course is designed to give you the required background material to be able to explore more advanced areas of mathematics. By now you have taken Algebra, Geometry, Calculus and perhaps a half-dozen other intimidating sounding math classes. In those classes you learned a certain aspect of mathematical problem solving. That is, you learned how to formulate a problem mathematically and solve it using the computational tools taught in those courses.

At this point in our mathematical education our focus shifts from being able to come up with the right answer to a problem to being able to *prove* that our techniques are correct. That is correct. We are going to prove things in this course.

Most advanced courses in mathematics requires us to precisely formulate our problems. And so we need a precise language to do this. It is this language that we will be learning in this course. We will learn the elementary rules of logic, set theory, equivalence relations, and functions and how these rules fit into our framework of mathematics.

Exams

There will be two in-class exams as well as a final cumulative exam. The exams will test your ability to work through some of the computations, your ability to apply the techniques to certain applications, as well as your ability to prove certain theorems using these techniques. The first exam is scheduled for Friday, September 29 and will count for 20 percent of your final grade. The second exam is scheduled for Friday, November 3 and will count for 20 percent of your final grade. The final exam will be held on Friday, December 15 from 9:00 a.m. to 11:30 a.m. The final will count for 20 percent of your final grade. There will be NO make-ups for missed exams. Please look over your schedule as soon as possible. If you see a potential conflict, inform me immediately.

Homework

The best way to learn Mathematics is to solve problems. Homework will be assigned at the end of each class period and collected the following class period. I will choose 4 or 5 problems to grade in each assignment. To earn full credit for a problem, a complete solution to the problem must be submitted. Just writing down the answer will not earn full credit. In addition to points for each graded problem, 5 points on each assignment will count for completeness and neatness of the graded assignment. Late assignments will not be graded, but they will be eligible for the 5 completion points. If you are not in class the day an assignment is collected, you may turn in your assignment into my office later that day. However, your assignment will be considered late. The homework is designed to help you identify where you might have difficulties. If you encounter any trouble with an assignment or a concept, seek help! The homework will count for 20% of your final grade.

Quizzes

Every other Friday, starting with September 8th, we will have an in-class quiz. There will be a total of 6 quizzes throughout the semester. You should treat the quizzes as mini-exams, covering material from approximately 6 days worth of course work. The quizzes will consists of 4 or 5 problems similar to problems from your graded homework, and they are to make sure that you are keeping up with the concepts presented in class, and to identify where you are having problems before you take the exams. The quizzes will count for 20% of your final grade.

Attendance

Attendance in MAT 305 is extremely important. Although there is no official attendance policy, note that if you are not in class on a particular day, your homework will not be graded for a score. I will also require that you be in class at 12:30 p.m. and no later. If you are late to class, you may stay to enjoy the wonderful learning experience. However, your homework assignment for the day will be considered late.

Grading

Your grade in this course will be based on three main factors: homework, quizzes and exams. The homework will be worth 20% of your final grade, the quizzes 20%, and the exams 60%. In addition to these factors, minor ethereal factors such attendance, class participation, attitude, and improvement over the course of the semester can also affect your grade. To determine your final grade, 90-100% = A, 80-89% = B, 70-79% = C, 60-69% = D, 59 and below = F, with the top two percents receiving a + and the bottom two percents receiving a -.

Calculators

Because this course is not computational based in any manner, the use of calculators is not allowed.

Important Dates

Monday, September 4 – Last Day to Drop/Add Friday, September 29 – Exam I Monday, October 9 – Autumn Break (no class) Tuesday, October 10 – Follow Monday Schedule Friday, November 3 – Exam II Friday, November 3 – Deadline for WD or P/F Wednesday, November 22 - Sunday, November 26 – Thanksgiving Break (no class) Friday, December 8 – Last Day of Classes Saturday, December 9 – Study Day Friday, December 15, 9:00 a.m. - 11:30 a.m. – Final Exam

Suggestions

Come to class with your homework assignment completed every day Study for at least 2 hours each day in addition to completing your homework assignment Read the section we will be covering in class *before* arriving to class Do not fall behind! Come to office hours to discuss homework and concepts. I am here to help! **Syllabus** MAT 305 : Fundamental Structures of Mathematics Fall 2006

| Week 1 | September 1 | Course Policies, Syllabus, Section 1.1 |
|---------|----------------|---|
| Week 2 | September 4 | Section 1.2 – Conditionals and Biconditionals |
| | September 8 | Section 1.3 – Quantifiers, Quiz I |
| Week 3 | September 11 | Section 1.4 – Basic Proof Methods I |
| | September 15 | Section 1.5 – Basic Proof Methods II |
| Week 4 | September 18 | Section 1.6 – Proofs Involving Quantifiers |
| | September 22 | Section 2.1 – Basic Concepts of Set Theory, Quiz II |
| Week 5 | September 25 | Section 2.2 – Set Operations, Review |
| | September 29 | Exam I |
| Week 6 | October 2 | Section 2.3 – Extended Set Operations and Indexed Families of Sets |
| | October 6 | Sections 2.4 – Induction |
| Week 7 | October 10^* | Sections 2.5 – Equivalent Forms of Induction |
| | October 13 | Section 2.6 – Principles of Counting, Quiz III |
| Week 8 | October 16 | Section 3.1 – Cartesian Products and Relations |
| | October 20 | Sections 3.2 – Equivalence Relations |
| Week 9 | October 23 | Section 3.3 – Partitions |
| | October 27 | Section 3.4 – Ordering Relations, Quiz IV |
| Week 10 | October 30 | Sections 4.1 – Functions as Relations, Review |
| | November 3 | Exam II |
| Week 11 | November 6 | Sections 4.2 – Constructions of Functions |
| | November 10 | Sections 4.3 – One-to-one and Onto Functions |
| Week 12 | November 13 | Section 4.4 – Images of Sets |
| | November 17 | Section 4.5 – Sequences, $\mathbf{Quiz} \ \mathbf{V}$ |
| Week 13 | November 20 | Section 5.1 – Equivalent Sets; Finite Sets |
| | November 24 | NO CLASS |
| Week 14 | November 27 | Sections 5.2 – Infinite Sets |
| | December 1 | Section 5.3 – Countable Sets |
| Week 15 | December 4 | Section 5.4 – The Ordering of Cardinal Numbers, $\mathbf{Quiz} \ \mathbf{VI}$ |
| | December 8 | Review |