For full credit on these problems, each must be submitted with a complete and clear solution, showing all of your work. You may work with other classmates on these problems, but please indicate on your assignment if you received help. Partial answers and incomplete solutions may be eligible for some partial credit, depending on the level of completeness and demonstrated understanding.

1. The group of all symmetries of a square is called $D_4$, the dyhedral group. If you label the vertices of the square 1 through 4, you can consider each symmetry as a permutation of $A = \{1, 2, 3, 4\}$.

   (a) How many elements does $D_4$ have?
   (b) Write out all elements of $D_4$ as permutations of $A$, and choosing effective notation for the permutations.
   (c) Make a group table for $D_4$ for the functional composition operation on $D_4$.
   (d) Make a Cayley diagram for the group $D_4$ using one reflection and one rotation as generators.
   (e) Is this group commutative? That is, does $a \circ b = b \circ a$ for all $a, b \in D_4$?
   (f) Is this group cyclic? That is, is there a particular symmetry that generates the entire dyhedral group?
   (g) Is this group “the same” as the group of symmetries of an 8 spoke pinwheel? Why or why not?